Mâu 1.2. Information on the new contributions of doctoral thesis

MINISTRY OF EDUCATION AND TRAINING **QUY NHON UNIVERSITY**

SOCIALIST REPUBLIC OF VIETNAM Independence – Freedom - Happiness

Binh Dinh, February 27th, 2024

INFORMATION

ON THE NEW CONTRIBUTIONS OF DOCTORAL THESIS

(Information will be posted on the Website)

Title: Simultaneous diagonalizations of matrices and applications for some classes of optimization

Speciality: Algebra and Number Theory

Code No.: 9460104

PhD student: Thi Ngan Nguyen

Course: 8

Advisors:

1. Advisor 1: Dr. Thanh-Hieu Le, Quy Nhon University;

2. Advisor 2: Prof. Ruey-Lin Sheu, National Cheng Kung University,

Taiwan.

Training institution: Quy Nhon University

NEW CONTRIBUTIONS OF THE THESIS

- 1. Completely solving the problem of simultaneous diagonalization via congruence (SDC) of Hermitian matrices, on both theoretical and practical aspects, by formulating the SDC problem as a semidefinite program (SDP). Specially, the SDC results of Hermitian matrices also hold for the real symmetric matrices. Specifically,
- a) Providing some necessary and sufficient SDC conditions for Hermitian matrices via an SDP;
- b) The proposing algorithm with polynomial complexity for solving the SDC problem of a finite collection of Hermitian matrices; illustrating the results by numerical experiments in MALAB:
- 2. Giving an alternative method, which is inductive and constructive, for solving the SDC problem of a finite collection of real symmetric matrices;
- 3. Applying the SDC results for completely computing the positive semidefinite interval of matrix pencil, which is then applied for
 - a) solving the generalized trust region subproblems: GTRS;
 - b) solving the quadratically constrained quadratic programming;
 - c) maximizing a sum of generalized Rayleigh quotients.

PhD Student

Dr. Thanh-Hieu Le

Thi Ngan Nguyen